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This application claims priority to USSN 60/236,765, filed September 29, 2000. The contents of this application are incorporated herein by reference in their entirety.

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studies in outbred populations, indicating that hundreds of thousands of individual SNPs will be required for a whole-genome scan.

In order to correct for multiple hypothesis testing, a significance level of 10^{-8} to 10^{-9} has been suggested, which implies a sample size requirement of several thousand individuals for adequate power to detect association. Although the costs involved in genotyping can be reduced by testing allele frequency differences between pools of DNA collected from individuals with extreme phenotypes, these tests are necessarily less powerful than individual genotyping and require even larger sample sizes.

Obtaining sample sizes sufficiently large for full-genome scans can be cumbersome and expensive. One approach for reducing the sample size requirements for pharmacogenomic studies is to focus on polymorphisms residing in a small set of candidate genes representing the drug target and the disease and drug response pathways. Sequencing a drug target gene in 100 individuals, for example, reveals polymorphisms present at a frequency of 2% or greater. These markers, usually SNPs, may then be used for association tests.

Haplotypes or diploid haplotype pairs constitute an alternative set of markers for an association test, and haplotype-based tests have been suggested for use in clinical studies. Nevertheless, haplotype-based tests require additional work relative to SNP-based tests, including direct sequencing or computational inference to identify haplotypes, and for now preclude less costly tests of pooled DNA. With the interest in haplotype-based tests growing, more guidance is needed by experimentalists weighing the relative merits of SNP-based and haplotype-based tests or choosing between tests based on haplotypes or haplotype pairs.

SUMMARY OF THE INVENTION

The invention provides a method of associating a phenotype with the occurrence of a particular set of allelic markers that occur at a plurality of genetic loci in a population of individuals. The invention allows for association tests to be performed using reduced sample sizes.

5 The method includes identifying the form of the allelic marker occurring at a plurality of genetic loci in the nucleic acid of each individual of the population, wherein each genetic locus is characterized by having at least two allelic forms of a marker and wherein the phenotype is expressed by a trait that is quantitatively evaluated on a numeric scale. A set of the allelic markers present in the nucleic acid of each individual of the population is identified, and the numeric value corresponding to the phenotypic trait for each individual of the population is obtained. Next, a p-value based on a particular set of markers and the numeric value is determined. The p-value provides the probability that the association of the phenotype with the particular set is due to a random association. A p-value less than a predetermined limit establishes the association of said phenotype with occurrence of a particular set of allelic markers that occur at a plurality of genetic loci in a population of individuals.

15 Any number of genetic loci can be examined using the methods of the invention. In some embodiments, the number of genetic loci is 2, 3, 4, 5, 10, 15, 20, 25, 50 or 100 or more. The number of individuals examined in the methods of the invention can be, e.g., 50,000 or fewer; 25,000 or fewer; 10,000 or fewer; 5,000 or fewer; 1,000 or fewer; 500 or fewer; 200 or fewer; 100 or fewer; 50 or fewer; or 25 or fewer.

20 In some embodiments, at least one allelic marker is a single nucleotide polymorphism (SNP). Various combinations of the allelic markers of at least two genetic loci that are in linkage disequilibrium with each other constitute different haplotypes.

In some embodiments, the genetic locus is characterized by having two allelic forms of the marker.

In some embodiments, at least two genetic loci are in linkage disequilibrium with respect to each other. The loci can be in partial or complete linkage disequilibrium.

25 In some embodiments, at least two genetic loci include a set of super-SNPs.

The p-value can be obtained, e.g., using a regression analysis, analysis of variance, or a combination of these methods. In some embodiments the p-value is less than 0.1. For example the p-value can be less than 0.05, 0.03, 0.01 or 0.005.

30 In another aspect, the invention provides a method of estimating the number of individual samples required to establish the association of a phenotype with occurrence of a particular set of allelic markers that occur at a plurality of genetic loci in a

population of individuals. The method includes determining the number of SNPs to be evaluated and combining consecutive SNPs that are in linkage disequilibrium into super-SNPs. The number of haplotypes is also determined, as is the estimated number of samples required.

5 In some embodiments, the number of SNPs plus the number of super-SNPs is smaller than the number of haplotypes, and estimating uses the formula provided on the last line of Table 1 in column 2 or column 3.

 In some embodiments, the number of SNPs plus the number of super-SNPs is greater than the number of haplotypes, and estimating uses the formula provided on the
10 last line of Table 1 in column 4.

 In some embodiments, the number of haplotypes is 2 or 3, and estimating uses the formula provided on the last line of Table 1 in column 4 or column 5. In other embodiments, the number of haplotypes is 4 or more, and estimating uses the formula provided on the last line of Table 1 in column 5.

15 In a still further aspect, the invention provides a method for identifying a genetic region associated with a disease. The method includes providing a plurality of single-nucleotide polymorphisms and a plurality of haplotypes for one or more regions of a chromosome, and identifying the number of single-nucleotide polymorphisms of said plurality in at least weak linkage disequilibrium with each other on said chromosomal
20 regions. The number of single-nucleotide polymorphisms in linkage disequilibrium is compared to the number of haplotypes in said chromosomal regions. A correlation test is then selected, wherein a single-nucleotide-based correlation test is selected if the number of single-nucleotide polymorphisms in linkage disequilibrium is smaller than the number of haplotypes and a number of haplotype-based correlation test is selected if the number
25 of single-nucleotide polymorphisms in linkage disequilibrium is greater than the number of haplotypes.

 In some embodiments, the haplotype-based correlation test is a regression test. In other embodiments, the haplotype-based correlation test is ANOVA test.

30 In another aspect, the invention provides a method for identifying a genetic region associated with responsiveness to an agent. The method includes providing a plurality of single-nucleotide polymorphisms and a plurality of haplotypes for one or more regions of

1 a chromosome and identifying the number of single-nucleotide polymorphisms of said
plurality in at least weak linkage disequilibrium with each other on said chromosomal
regions. The number of single-nucleotide polymorphisms in linkage disequilibrium is
compared to the number of haplotypes in said chromosomal regions; and a correlation
5 test is selected. A single nucleotide-based correlation test is selected if the number of
single-nucleotide polymorphisms in linkage disequilibrium is smaller than the number of
haplotypes, thereby identifying a genetic region associated with responsiveness to an
agent.

10 In some embodiments, the haplotype-based correlation test is a regression test. In
other embodiments, the haplotype-based correlation test is ANOVA test.

15 The invention provides efficient and cost-effective association tests based on
SNPs and haplotypes. Also provided by the invention are methods of association
employing quantitative traits characteristic of disease risk or clinical response using SNP-
based and haplotype-based tests. A further advantage of the invention is that allows for
association tests to be performed using reduced sample sizes.

20 Unless otherwise defined, all technical and scientific terms used herein have the
same meaning as commonly understood by one of ordinary skill in the art to which this
invention belongs. Although methods and materials similar or equivalent to those
described herein can be used in the practice or testing of the invention, suitable methods
and materials are described below. All publications, patent applications, patents, and
other references mentioned herein are incorporated by reference in their entirety. In the
case of conflict, the present specification, including definitions, will control. In addition,
the materials, methods, and examples are illustrative only and not intended to be limiting.

25 Other features and advantages of the invention will be apparent from the
following detailed description and claims.

BRIEF DESCRIPTION OF THE DRAWINGS

FIG. 1 is a graphic representation showing the expected significance levels for
tests of 150 individuals, corrected for multiple hypothesis testing, are shown for a
30 haplotype-based ANOVA test (thin dot-dash) and for haplotype-based (thick dot-dash),

SNP-based (dash), and super-SNP-based (solid) regression tests. Smaller p-values are more significant. In the model, $G = 10$ SNPs contribute a cumulative 5% to the total variance of a quantitative phenotype. The abscissa of the top panel, G/Γ , represents the extent of linkage disequilibrium as measured by consecutive correlated SNPs, and is related to the number of haplotypes H by $\Gamma = \log_2 H$.

FIG. 2 is a graphic representation showing the sample size N required for a Type I error rate of 5%, corrected for multiple hypothesis testing, and 80% power to reject the null hypothesis, is shown for a haplotype-based ANOVA test (thin dot-dash) and for haplotype-based (thick dot-dash), SNP-based (dash), and super-SNP-based (solid) regression tests. In the model, $G = 10$ SNPs contribute a cumulative 5% to the total variance of a quantitative phenotype. The abscissa of the top panel, G/Γ , represents the extent of linkage disequilibrium as measured by consecutive correlated SNPs, and is related to the number of haplotypes H by $\Gamma = \log_2 H$.

FIGS. 3A-3F. is a graphic representation showing comparisons between SNP-based and haplotype-based tests, the total number of SNPs is fixed at 20. The number of causative SNPs is 1 (left panels, 3A and 3D), 3 (middle panels, 3B and 3E), or 10 (right panels, 3C and 3F). The number of haplotypes, H , is varied from 1 to 100 within each panel. The additive variance per SNP is fixed at 0.025. The top series of panels illustrates the expected significance for a fixed population size of 300, and the bottom series illustrates the population size required to attain a p-value of 0.05 (5% false-positive rate including the multiple-testing correction) and a power of 0.8 (20% false-negative rate), for the haplotype-pair ANOVA test (dot-dashed line), the haplotype regression test (dashed line), and the SNP regression test (solid line). Haplotype-based tests and SNP-based tests cross in power when the number of haplotypes is just larger than the number of causative SNPs.

FIGS. 4A-4F. Same as FIG. 3, except the total additive variance is fixed at 0.075, implying an additive variance per SNP that varies from 0.075 (1 causative SNP) to 0.0075 (10 causative SNPs). The number of causative SNPs is 1 (left panels, 4A and 4D), 3 (middle panels, 4B and 4E), or 10 (right panels, 4C and 4F). The number of haplotypes, H , is varied from 1 to 100 within each panel. Haplotype-based tests and SNP-

based tests cross in power when the number of haplotypes is just larger than the number of causative SNPs.

DETAILED DESCRIPTION OF THE INVENTION

5 The present invention provides methods for associating phenotypes with particular sets of allelic markers. The methods are based in part on an analysis of the relative power of association tests based on SNPs and haplotypes. The methods are particularly suitable for identifying quantitative traits characteristic of disease risk or clinical response. The methods described herein provide for simple, analytical estimates
10 of the relative efficiency of SNP-based and haplotype-based tests.

 The present invention discloses the power of association studies using regression tests and ANOVA to identify SNP-based and haplotype-based markers for quantitative traits. Results derived from analytic theory based on an underlying variance components model indicate that ANOVA tests of haplotype pairs should only be used when the
15 number of haplotypes is small. When the number of haplotypes increases beyond 4 or 5, a haplotype-based regression test has greater power. When the extent of linkage disequilibrium is difficult to establish, haplotype-based tests are more powerful than SNP-based tests if the number of haplotypes is less than the number of SNPs, while SNP-based tests are more powerful if there are fewer SNPs than haplotypes. The latter
20 condition almost certainly holds when large genomic regions are tested for association. When the extent of linkage disequilibrium is evident because of correlations between individual SNPs, regression tests performed using super-SNPs, blocks of correlated SNPs, have the greatest power.

 Simple formulas are provided for the experimentalist to estimate sample size
25 requirements and p-values under each of these tests. It is shown in the Examples that these predictions agree with literature comparisons between SNP-based and haplotype-based tests, including findings that tests based on multi-locus markers, here termed super-SNPs, can have greater power than tests based on SNPs alone. The invention also provides that increasing the sample size of a study is more important than increasing the

number of SNPs once the density of SNPs is comparable to the length scale of linkage disequilibrium.

While stronger linkage disequilibrium between SNPs implies fewer haplotypes, a small number of haplotypes does not necessarily imply strong linkage. A better estimate of the extent of linkage disequilibrium may be the typical number of consecutive SNPs correlated between different haplotypes, as demonstrated in Example 2.

Overall, the invention provides a simple set of guidelines for designing an association test for a candidate gene or drug target. First, identify the SNPs or haplotypes for one or more candidate genes. Consecutive SNPs found to be in linkage disequilibrium should be combined into a single super-SNP. When the number of SNPs and super-SNPs is smaller than the number of haplotypes, the SNP-based regression test is more powerful and should be used to calculate the required sample sizes; otherwise, haplotype-based tests are more powerful. With two or three haplotypes, the ANOVA test and the regression test have similar power and may both be used to estimate sample size requirements. With four or more haplotypes, the regression test is more powerful and should be used instead of ANOVA.

SNP-based phenotype models

A variance components model is used to describe the dependence of an individual's phenotype on its genotype (Falconer et al., Introduction to Quantitative Genetics. Prentice Hall, New York (1996)). This quantitative model may also be applied to a haplotype relative risk model for disease susceptibility in which the risk from haplotypes are multiplicative and each risk factor is proportional to an exponential of an underlying quantitative trait (Terwilliger et al., Hum. Hered. 42: 337-346, 1992).

In the variance components model, the quantitative phenotype is denoted X and is standardized to have zero mean and unit variance. Several quantitative trait loci, here modeled as biallelic markers or SNPs, are assumed to contribute to the phenotypic value. Individual SNPs may occur within the same gene, and the total number of SNPs is G . The alleles for a particular SNP γ , $\gamma = 1$ to G , are labeled $A_{\gamma 1}$ and $A_{\gamma 2}$, with respective frequencies p_{γ} and $1 - p_{\gamma 1}$ in an unselected population. Hardy-Weinberg equilibrium is assumed separately for each SNP (but not for the joint distribution of SNPs γ and γ'), and

the probabilities of the genotypes $A_{\gamma 1}A_{\gamma 1}$, $A_{\gamma 1}A_{\gamma 2}$, and $A_{\gamma 2}A_{\gamma 2}$ are therefore p_{γ}^2 , $2p_{\gamma}(1-p_{\gamma})$, and $(1-p_{\gamma})^2$. The frequency of allele $A_{\gamma 1}$ for each individual is either 1, 0.5, or 0, and is denoted f_{γ} . The variance of f_{γ} is denoted $\sigma_{f_{\gamma}}^2$, with

$$\sigma_{f_{\gamma}}^2 = p_{\gamma}^2 \cdot (1) + 2p_{\gamma}(1-p_{\gamma}) \cdot (1/4) + (1-p_{\gamma})^2 \cdot (0) = p_{\gamma}(1-p_{\gamma})/2.$$

5 The effect of allele $A_{\gamma 1}$ is assumed to be purely additive with respect to allele frequency, a shift of $a_{\gamma}/2$ for each copy inherited. The shifts in phenotypic value are therefore $a_{\gamma}-\mu_{\gamma}$ for the $A_{\gamma 1}A_{\gamma 1}$ homozygote, $-\mu_{\gamma}$ for the heterozygote, and $-a_{\gamma}-\mu_{\gamma}$ for the $A_{\gamma 2}A_{\gamma 2}$ homozygote, where the constant $\mu_{\gamma} = a_{\gamma}(2p_{\gamma} - 1)$ ensures that X has zero mean. This SNP contributes a phenotypic variance of σ_{γ}^2 ,

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$$\sigma_{\gamma}^2 = 2p_{\gamma}(1-p_{\gamma})a_{\gamma}^2,$$

to the total phenotypic variance of 1. For a polygenic trait, the variance σ_{γ}^2 contributed by any individual SNP is small compared to the residual variance $1 - \sigma_{\gamma}^2 \approx 1$ from other genetic and environmental factors. The expected value of σ_{γ}^2 is defined as σ_G^2 ,

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$$\sigma_G^2 = G^{-1} \sum_{\gamma=1}^G \sigma_{\gamma}^2,$$

the mean of the individual variances. The fractional variance explained by all the SNPs together, $G\sigma_G^2$, may also be much smaller than 1. Note that if the effect of a particular SNP is not purely additive, an additive effect can nevertheless be constructed by defining a_{γ} as half the difference in phenotypic shift between $A_{\gamma 1}$ and $A_{\gamma 2}$ homozygotes minus $d_{\gamma} \cdot (2p_{\gamma} - 1)$, where d_{γ} is the difference between the phenotype shift for heterozygotes and the midpoint of the shifts for homozygotes. This approach is generally valid for alleles with dominant, recessive, or multiplicative effects; it fails only for very rare recessive alleles and, correspondingly, for very common dominant alleles. In these extreme cases, however, the additive variance vanishes and associations are difficult to detect without

25 recourse to highly selected populations.

Haplotypes

The G individual SNPs may occur in up to 2^G distinct allelic combinations. Due to linkage disequilibrium, however, a smaller subset of H haplotypes are assumed to occur in a test population. Using η to label the haplotype, $\eta = 1$ to H , the phenotypic shift for an individual with haplotypes η and η' is defined in analogy to the SNP shifts as $(a_\eta + a_{\eta'})/2$, where

$$a_\eta = \sum_{\gamma=1}^G [P(A_{\gamma 1}|\eta) - P(A_{\gamma 2}|\eta) - (2p_\gamma - 1)] a_\gamma.$$

The term $P(A_{\gamma 1}|\eta)$ has value 1 if haplotype η has allele $A_{\gamma 1}$ and is 0 otherwise. Similarly, $P(A_{\gamma 2}|\eta) = 1$ if haplotype η has allele $A_{\gamma 2}$ and is 0 otherwise. The difference in these terms, either +1 or -1, less its mean value $2p_\gamma - 1$, multiplies a_γ to yield the phenotypic shift in haplotype η due to the phase of SNP γ and is summed over all G SNPs.

While the precise value of a_η depends on the particular alleles occurring in haplotype η , the distribution of values of a_η may be estimated by considering the term $P(A_{\gamma 1}|\eta) - P(A_{\gamma 2}|\eta)$ to be a random variable taking the value +1 with probability p_γ and the value -1 with probability $1-p_\gamma$. This mean probability approximation recovers the SNP allele frequencies p_γ and ensures that the mean of a_η is zero. The variance $\text{Var}(a_\eta)$ may be obtained under a random phase approximation in which the directions of the shifts a_γ are uncorrelated. With this assumption, the variance of the sum over SNPs is the sum of the individual variances even if the SNP allele frequencies are correlated. The variance of a_η arising from SNP γ is

$$p_\gamma[1-(2p_\gamma-1)]^2 a_\gamma^2 + (1-p_\gamma)[-1-(2p_\gamma-1)]^2 a_\gamma^2 = 4p_\gamma(1-p_\gamma)a_\gamma^2 = 2\sigma_\gamma^2.$$

The final variance for the distribution of haplotype-dependent shifts a_η is

$$\text{Var}(a_\eta) = 2G\sigma_G^2,$$

where σ_G^2 is the mean SNP variance as previously defined.

The mean phenotypic shift contributed by haplotype η is $p_\eta^2 a_\eta + 2p_\eta(1-p_\eta)(a_\eta/2)$, or simply $p_\eta a_\eta$. The phenotypic variance contributed by this haplotype is defined as σ_η^2 , $\sigma_\eta^2 = p_\eta^2 a_\eta^2 + 2p_\eta(1-p_\eta)(a_\eta/2)^2 - (p_\eta a_\eta)^2 = (1/2)p_\eta(1-p_\eta)a_\eta^2$.

When the number of haplotypes is large, the probability p_η for each haplotype is small and $\sigma_\eta^2 \approx p_\eta a_\eta^2 / 2$. The mean value of σ_η^2 is defined as σ_H^2 ,

$$\sigma_H^2 = H^{-1} \sum_{\eta=1}^H \sigma_\eta^2 = H^{-1} \sum_{\eta=1}^H p_\eta a_\eta^2 / 2 = (G/H) \sigma_G^2,$$

where it is assumed that p_η and a_η are uncorrelated. Note that the total haplotype-based phenotypic variance, $H\sigma_H^2$, equals the total SNP-based phenotypic variance, $G\sigma_G^2$.

In the special case that only one of the SNPs has a non-zero phenotypic shift a_γ , each haplotype η will have a phenotypic shift a_η of either $2(1-p_\gamma)a_\gamma$ or $-2p_\gamma a_\gamma$, depending on whether $A_{\gamma 1}$ or $A_{\gamma 2}$ is included. The corresponding values for σ_η^2 will be $p_\eta(1-p_\eta)\sigma_\gamma^2$ multiplied by either $p_\gamma/(1-p_\gamma)$ or $(1-p_\gamma/p_\gamma)$. Assuming that $A_{\gamma 1}$ is the minor allele with p_γ much smaller than 1 and that the haplotype frequency p_η is also much smaller than 1, $\sigma_\eta^2 = (p_\eta/p_\gamma)\sigma_\gamma^2$ is the result for the variance due to the haplotype. A reasonable assumption is that the ratio p_η/p_γ is close to $(1/H)/(1/G)$, yielding $\sigma_\eta^2 = (G/H)\sigma_\gamma^2$ as before.

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Super-SNPs

When the number of haplotypes H is significantly smaller than the number of SNPs G , linkage disequilibrium must exist between certain of the SNPs. The extent of linkage disequilibrium between a pair of SNPs γ and γ' is traditionally expressed in terms of the factor $\rho_{\gamma\gamma'}^2$,

$$\rho_{\gamma\gamma'}^2 = (p_{11}p_{22} - p_{12}p_{21})^2 / [p_\gamma(1-p_\gamma)p_{\gamma'}(1-p_{\gamma'})],$$

where p_{ij} is the frequency with which alleles $A_{\gamma i}$ and $A_{\gamma' j}$ appear in phase on the same chromosome and, as before, p_γ and $p_{\gamma'}$ are the frequencies of the $A_{\gamma 1}$ and $A_{\gamma' 1}$ alleles.

When the minor-allele frequencies of the two SNPs are identical, the factor ρ^2 ranges from 1 for complete linkage to 0 for no correlation.

When linkage disequilibrium exists, the additive variance measured for a SNP-based marker may include contributions from other SNPs. The observed additive variance for a SNP γ , denoted $\sigma_\gamma^2(\text{obs})$, is

$$\sigma_y^2(\text{obs}) = \sum_{\gamma=1}^G \rho_{\gamma\gamma}^2 \sigma_{\gamma}^2,$$

where the terms σ_{γ}^2 are the underlying SNP-based variance components and include the self-contribution σ_{γ}^2 . This is the precise relationship used to analyze association tests of neutral markers in linkage disequilibrium with causative mutations Ott et al., Analysis of Human Genetic Linkage, Johns Hopkins University Press, Baltimore, 1999; Falconer et al., Introduction to Quantitative Genetics, Prentice Hall, New York, 1996)

The expected value of $\sigma_y^2(\text{obs})$ is estimated by noting that H haplotypes correspond to complete equilibrium between an effective number of Γ polymorphisms such that $2^{\Gamma} = H$, or $\Gamma = \log_2 H$. This suggests that linkage disequilibrium between SNPs extends approximately G/Γ SNPs, beyond which SNPs are essentially uncorrelated. The extremes are weak linkage, $G/\Gamma = 1$, and strong linkage, $G/\Gamma = 1$.

A simple model spanning the regime from weak linkage to strong linkage is that the G SNPs exist in Γ blocks of G/Γ SNPs, with perfect correlation within blocks and no correlation between blocks. The perfectly-correlated blocks are termed super-SNPs, and each SNP within a super-SNP has an identical observed additive variance. The use of a similar type of structure, termed a trimmed haplotype, has been previously suggested in the context of linkage analysis (MacLean et al., *Am. J. Hum. Genet.* 66:1062-75, 2000). If sequence data are available, then the extent of linkage disequilibrium G/Γ may be related to the average number of SNPs over which two haplotypes remain in phase.

The expected variance for a super-SNP is termed σ_r^2 , equal to the variance $\sigma_y^2(\text{obs})$ observed for any of its component correlated SNPs. Furthermore, because of the correlation within a super-SNP block,

$$\sigma_r^2 = (G/\log_2 H) \sigma_G^2,$$

where $G/\log_2 H$ is the number of SNPs within the block. Because the blocks are

uncorrelated, the variance summed over super-SNPs is identical to the variance summed over SNPs or haplotypes,

$$\Gamma \sigma_r^2 = G \sigma_G^2 = H \sigma_H^2.$$

Since $\Gamma = \log_2 H$, Γ is smaller than H and the phenotype variance explained by a super-SNP is expected to be larger than that explained by a haplotype. Also, since the number

of haplotypes $H \leq 2^G$, Γ is usually smaller than G and a typical super-SNPs explain more phenotypic variance than does a typical SNPs.

Extreme phenotypic variance

5 Association tests are most sensitive to markers, here SNPs, haplotypes, and super-SNPs, conferring the greatest variation to the phenotype. Here the expectations for these extreme values are related to the variance terms σ_G^2 , σ_H^2 , and σ_I^2 for the various markers.

Under the phenotype model, the set of phenotypic shifts for M markers, either G SNPs, H haplotypes, or Γ super-SNPs, is drawn from a normal distribution with
 10 variance denoted σ_M^2 . The probability that the largest positive shift confers a variance smaller than an extreme value σ_{ex}^2 is $[\Phi(\sigma_{ex}/\sigma_M)]^M$, where $\Phi(z)$ is the cumulative standard normal distribution for normal deviate z (Weisstein, The CRC Concise Encyclopedia of Mathematics. CRC Press, Boca Raton (1999). The expected median for the extreme value is obtained by setting $[\Phi(\sigma_{ex}/\sigma_M)]^M$ to 0.5. The median grows very
 15 slowly with the number of markers. For 5 markers, the result is $(\sigma_{ex}/\sigma_M) = 1.13$; for 10 markers, $(\sigma_{ex}/\sigma_M) = 1.50$; and for 100 markers, $(\sigma_{ex}/\sigma_M) = 2.46$. The slow growth may be derived from the asymptotic expansion of $\Phi(z)$ valid for large z (Mathews et al., Mathematical Methods of Physics, Second Edition. Benjamin/Cummings, London. (1970)).

20 $\Phi(z) \approx 1 - (2\pi z^2)^{-0.5} \exp(-z^2/2) \approx \exp[-(2\pi z^2)^{-0.5} \exp(-z^2/2)].$

The approximate implicit solution for σ_{ex} is

$$(\sigma_{ex}/\sigma_M)^2 \approx 2 \ln[M / (2\pi)^{0.5} z \ln(2)] \text{ with only a logarithmic dependence on } M.$$

The simplifying assumption is made that $\sigma_{ex} \approx \sigma_M$ and use the root-mean-square variance
 25 as an estimate of the extreme value. A similar approximation for the most extreme positive shift a_η for a haplotype is the standard deviation of the distribution for a_η , or $(2H\sigma_H^2)^{0.5}$. The corresponding most extreme negative shift is $-(2H\sigma_H^2)^{0.5}$.

Regression test for association

A suitable test statistic for either association of a SNP-based or haplotype-based marker with a quantitative phenotype is the coefficient b_1 for a regression model of the phenotypic value on the marker dose ((Falconer et al., 1996; SNEDECOR et al.,

5 Statistical Methods, Eighth Edition. Iowa State University Press, Ames (1989))

$$X_i = b_1 \delta f_i + \varepsilon_i.$$

The N individuals included in the sample are specified by the index i . The difference between the marker frequency in individual i and in the total sample is δf_i , and the residual ε_i is uncorrelated with δf_i . The expected value for b_1 is

10 $b_1 = \sigma_M / \sigma_f,$

where σ_M^2 is the additive variance of the marker, either $\sigma_r^2(\text{obs})$ for a SNP-based test or σ_η^2 for a haplotype-based test, and σ_f^2 is the variance of the marker frequency and equals $p(1-p)/2$ for a marker under Hardy-Weinberg equilibrium with frequency p . Since the variance of ε_i is close to 1 when σ_M^2 is small, the variance of the estimator for b_1 , σ_b^2 , is

15 the same under the null hypothesis, $b_1 = 0$, and the alternative hypothesis, $b_1 > 0$, and $\sigma_b^2 = 1 / N \sigma_f^2$ for a one-sided test.

Combining the expected value for the regression coefficient with the standard deviation of the estimator, the expected p-value for a one-tailed test for a marker with

20 additive variance σ_M , using a Bonferroni correction for M multiple tests, is

$$\text{p-value} = 1 - [\Phi(N^{0.5} \sigma_M)]^M. \quad (1)$$

Using the asymptotic expansion for $\Phi(z)$ yields

$$\text{p-value} \approx M (2\pi N \sigma_M^2)^{-0.5} \exp(-N \sigma_M^2 / 2) \text{ as an approximation valid for small p-values.}$$

For a corrected final Type I error rate of α , the uncorrected p-value for a

25 significant finding must be smaller than α/M . The Type II error rate β has no multiple testing correction. Defining the normal deviates $z_{\alpha/M} = \Phi^{-1}(1-\alpha/M)$ and $z_{1-\beta} = \Phi^{-1}(\beta)$, the resulting sample size required to detect a marker contributing phenotypic variance σ_M^2 with power $1-\beta$ is

$$N_{\text{REGR}} = (z_{\alpha/M} - z_{1-\beta})^2 / \sigma_M^2. \quad (2)$$

A simplified approximation for the sample size may be obtained by noting that $z_{\alpha/M}$ is typically larger than $z_{1-\beta}$. When $\alpha = 0.05$, $M = 10$, and $1-\beta = 0.8$, for example, $z_{\alpha/M} = 2.58$ while $z_{1-\beta} = -0.84$. Neglecting $z_{1-\beta}$ relative to $z_{\alpha/M}$ (or setting the power to 50%) yields

$$5 \quad N \approx 2 \ln(M/\alpha) / \sigma_M^2.$$

The logarithmic term arises from the asymptotic expansion $z_\alpha \sim 2 \ln(1/\alpha)$ valid for small α .

ANOVA test for haplotype association

10 Analysis of variance (ANOVA) may also be used to test for association between haplotype pairs and a quantitative phenotype. In a typical ANOVA test, N individuals are sorted into $K = H(H+1)/2$ distinct haplotype pairs and the between-genotype phenotypic variance is compared to the within-genotype phenotypic variance. A significant finding in an ANOVA test is approximately equivalent to detecting a significant difference in

15 mean phenotype value for at least one of the $C = K(K-1)/2$ possible pairwise comparisons. The most significant finding will typically arise from the difference Δ in mean phenotypic value between the pair of genotypes with the most extreme positive and negative shifts.

20 The expected maximum difference Δ is obtained from the distribution of a_η as

$$\Delta = 2[\text{Var}(a_H)]^{0.5}, \text{ or } (8H\sigma_H^2)^{0.5}. \text{ The variance for this test statistic is}$$

$$\sigma^2 = \sigma_R^2[(1/n)+(1/n')],$$

where n and n' are the number of individuals in the total sample size of N in the two extreme classes. Under the mean probability approximation, each p_η is $1/H$. If the most

25 extreme phenotypic shifts correspond to homozygous genotypes, then n and n' are both approximately N/H^2 and the variance is $\sigma^2 = 2H^2/N$. If the genotypes with extreme phenotype values are both heterozygous, the variance is H^2/N . The additive model suggests that homozygotes will be at least tied for the maximum phenotypic shift. The p-value for the comparison of extreme phenotypes is

$$30 \quad \text{p-value} = 1 - [\Phi(\Delta/\sigma)]^C = 1 - [\Phi(2\sigma_H N^{0.5} J^{0.5}/H^{0.5})]^C, \quad (3)$$

where the factor of C is the correction for multiple hypothesis testing and $J = 1$ if homozygotes are extreme, 2 if heterozygotes are extreme, and 1.5 if one homozygote and one heterozygote are extreme.

5 As with the regression test, the residual variance σ_R^2 is close to 1, and an expression yielding the required sample size is $1/\sigma^2 = (z_{\alpha/C} - z_{1-\beta})^2 / \Delta^2$, or

$$N_{ANOVA} = (z_{\alpha/C} - z_{1-\beta})^2 H/4J\sigma_H^2. \quad (4)$$

The ratio N_{ANOVA}/N_{REGR} of the sample size required for an ANOVA test, relative to that required for a series of H regression tests, is obtained from the ratio of Eq. 4 to Eq. 2. An

10 estimate for this ratio, valid when $z_{\alpha/C}$ and $z_{\alpha/H}$ are both large compared to $z_{1-\beta}$, is

$$N_{ANOVA}/N_{REGR} \approx (H/4J) \ln(C/\alpha)/\ln(H/\alpha).$$

The logarithmic dependence varies slowly, and the factor $H/4J$ explains most of the relative efficiency. When the number of haplotypes is small, ANOVA is more powerful. A cross-over occurs near $H = 4$ if homozygotes are extreme and near $H = 8$ if

15 heterozygotes are extreme. Beyond the cross-over, the regression test is more powerful.

Comparison of tests using SNPs, haplotypes, and super-SNPs

The significance levels expected for an association test and the sample level required to attain a pre-specified significance threshold are compared for statistical tests

20 based on SNPs, haplotypes, and super-SNPs. The regression test is applied to all three, and the haplotype-based ANOVA test assuming homozygotes are most extreme is analyzed as well. A summary of the equations used for this analysis is provided in Table I.

Table I. Summary of association tests

Marker type	SNP	Super-SNP	Haplotype	Haplotype
Test	Regression	Regression	Regression	ANOVA
Number of markers	G	$\Gamma \approx \log_2 H$ or $G / (\# \text{ of consecutive correlated SNPs})$	H	H

Phenotypic variance explained by markers	$G\sigma_G^2$	$\Gamma\sigma_r^2$	$H\sigma_H^2$	$H\sigma_H^2$
Observed variance per marker	σ_G^2 (weak linkage) or σ_r^2 (strong linkage)	$\sigma_r^2 = (G/\Gamma)\sigma_G^2$	$\sigma_H^2 = (G/H)\sigma_G^2$	σ_H^2
p-value for N individuals	$1 - [\Phi(N^{0.5}\sigma_G)]^G$ (weak linkage) or $1 - [\Phi(N^{0.5}\sigma_r)]^G$ (strong linkage)	$1 - [\Phi(N^{0.5}\sigma_r)]^\Gamma$	$1 - [\Phi(N^{0.5}\sigma_H)]^H$	$1 - \{\Phi[2(NJ/H)^{0.5}\sigma_H]\}^C$ with $J = 1, 1.5$ or 2 ; $C = K(K-1)/2$; and $K \approx H(H+1)/2$
N for Type I error α and power $1-\beta$	$(z_{\alpha/G} - z_{1-\beta})^2/\sigma_G^2$ (weak linkage) or $(z_{\alpha/G} - z_{1-\beta})^2/\sigma_r^2$ (strong linkage)	$(z_{\alpha/\Gamma} - z_{1-\beta})^2/\sigma_r^2$	$(z_{\alpha/H} - z_{1-\beta})^2/\sigma_H^2$	$(z_{\alpha/C} - z_{1-\beta})^2 H/4J\sigma_H^2$

The number of SNPs, G , is set to 10 for these examples, and the fraction of the total phenotypic variance explained by these 10 SNPs, $G\sigma_G^2$, is 5%. This relatively large value reflects a model in which SNPs in a known drug target are tested for association with drug response. The number of haplotypes, H , is varied from a maximum of 1024, no linkage between SNPs, to a minimum of 2, complete linkage disequilibrium. The number of super-SNPs, Γ , is $\log_2 H$, and the extent of linkage disequilibrium measured in SNPs, G/Γ , varies from 1 (no linkage) to 10 (complete disequilibrium). The mean phenotypic variance contributed per haplotype, σ_H^2 , is $(G/H)\sigma_G^2$, and the observed variance per SNP and the mean variance per super-SNP are both $\sigma_r^2 = (G/\Gamma)\sigma_G^2$.

The expected p-values from an association study with a sample size $N = 150$ using these three types of markers, obtained from Eq. 1 for regression tests and Eq. 3 for ANOVA, is displayed in FIG. 1. The abscissas of the top and bottom panels are related by $G/\Gamma = \log_2 H$. The general behavior for each test is a gain in significance as linkage disequilibrium increases from left to right across the figure. The test providing the smallest p-value uses super-SNPs, followed by the SNP-based test and the haplotype-based regression test. The haplotype-based ANOVA test has less significance than the haplotype-based regression test until there are only 2 or 3 haplotypes, at which point the p-values cross and the ANOVA test is better.

The ratio $p\text{-value}(\text{SNP})/p\text{-value}(\text{super-SNP})$ reduces to the extent of linkage disequilibrium measured by G/Γ . The test are equally significant when $G/\Gamma = 1$ and all SNPs are uncorrelated. The super-SNP test is 10-fold more significant when $G/\Gamma = 10$, complete disequilibrium across the 10 SNPs. If super-SNPs can be identified and the number of super-SNPs is smaller than the number of haplotypes, then the super-SNP test produces a more significant finding than the haplotype test.

If the extent of linkage disequilibrium is difficult to estimate or super-SNPs can not be identified, then it is more reasonable to compare the p-value from a haplotype test based on the observed number of haplotypes to the p-value from a SNP-based test with no linkage disequilibrium, corresponding to $G/\Gamma = 1$. The ratio of these p-values is $p\text{-value}(\text{HAP})/p\text{-value}(\text{SNP}) = (H/G)^{3/2} \exp[N\sigma_G^2(1-G/H)/2]$, an approximation obtained from the asymptotic expansion of $\Phi(z)$ for small z . The haplotype-based test is more significant when the number of haplotypes is smaller than the number of SNPs. Conversely, the SNP-based test is more significant when the number of SNPs is smaller than the number of haplotypes.

The sample sizes required to achieve a power $1-\beta = 80\%$ to reject the null hypothesis with a Type I error rate $\alpha = 5\%$ corrected for multiple hypothesis testing are shown in FIG. 2. As in FIG. 1, the top and bottom panels are identical except for a rescaling of the abscissa. The power of each test increases with the linkage disequilibrium from left to right. When the linkage is virtually complete, with only 2 or 3 haplotypes in a population, the haplotype-based ANOVA test is more powerful than the haplotype-based regression test. With slightly less disequilibrium, however, the ANOVA test loses power rapidly.

The most powerful regression test uses super-SNPs, followed by SNP-based and haplotype-based tests. An approximate value for the ratio of the sample sizes required for the SNP-based and super-SNP-based tests is

$$N_{\text{SNP}}/N_{\text{SSNP}} = \ln(G/\alpha) / \ln(\Gamma/\alpha),$$

rising from a factor of 1 under weak linkage to a maximum of $1 + \log_{1/\alpha}(G)$ under strong linkage. If the extent of linkage disequilibrium is evident and super-SNPs can be identified, the test based on super-SNPs is uniformly more powerful than the haplotype-based test. If linkage disequilibrium is difficult to estimate, then it is reasonable to

compare the sample size required by the haplotype-based test for H haplotypes to the sample size required for the SNP-based test assuming the worst case of no disequilibrium. This ratio may be approximated as

$$N_{\text{HAP}}/N_{\text{SNP}} = (H/G) \ln(H/\alpha) / \ln(G/\alpha).$$

- 5 Haplotype-based tests are more efficient than SNP-based tests when there are fewer haplotypes than SNPs and less efficient when there are more haplotypes than SNPs.

Sample size estimates for other values of the fractional variance contributed by the polymorphisms, fixed at 5% in this example, may be readily determined from FIG. 1 because N is inversely proportional to this variance.

- 10 Additional embodiments are within the claims.

The invention will be further illustrated in the following non-limiting examples.

EXAMPLE 1 COMPARISON OF ASSOCIATION STUDIES AT THE GENE ENCODING THE β_2 -ADRENERGIC RECEPTOR (β_2 AR)

- 15 This example concerns association studies using the gene encoding the β_2 -adrenergic receptor (β_2 AR). This G-protein coupled receptor is expressed in airway smooth muscle cells and mast cells and is the target of bronchodilating β -agonists such as isoprenaline, salmeterol, and albuterol used in the treatment of asthma [Goodman and Gilman's The Pharmacological Basis of Therapeutics, Ninth Edition. Goodman LS, Hardman JG, Limberd LE, Molinoff PB, Ruddon RW, Gilman AG (Eds.). McGraw Hill, 20 New York (1996)]. Polymorphisms at codons 16 (arg to gly) and 27 (gln to glu) have been associated at varying levels of significance with response to β -agonist treatment [Tan *et al.*, Lancet. 350: 995-999, 1997; Taylor *et al.*, Thorax. 55: 762-767, 2000; Chong *et al.*, Pharmacogenetics.10:153-162, 2000; Liggett, J. Allergy Clin. Immunol. 105:S487-S492, 2000]. Between the β_2 AR transcription start site and the intronless 25 coding region is a 5'-leader cistron which encodes a 19-aa peptide, and polymorphisms in this region have been shown to affect β_2 AR expression [McGraw *et al.*, J. Clin. Invest. 102: 1927-1932, 1998]. To understand the relevance of these and other polymorphisms in β_2 AR, Liggett and coworkers undertook an association study focusing on the relationship between SNPs, haplotypes, and response to the bronchodilator albuterol [Drysdale *et al.*, 30 Proc. Natl. Acad. Sci. USA 97: 10483-10488, 2000].

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In a scan of chromosomes from 23 Caucasians, 19 African-Americans, 20
Asians, and Hispanic-Latinos, the Liggett study identified a total of 13 polymorphic sites
in a region including ~700 nt of ORF and ~1100 nt of 5' UTR, including the 5'-leader
cistron. While 12 total haplotypes were identified, only 4 had frequency above 5% in any
5 ethnicity, and only 3 of these occurred at 2% frequency or greater in the Caucasian
population. In these 3 haplotypes, 10 of the 13 SNPs were variable. The SNPs and
haplotypes were then tested for association with albuterol response, adjusted for sex and
baseline severity, in a population of 121 Caucasian patients with moderate asthma. A
haplotype association test was performed using ANOVA for the 5 haplotype pairs
10 observed in the treated population, and SNP main effects were tested using ANOVA for
SNP genotypes with p-values corrected for multiple hypothesis testing. While the
haplotype-based test yielded a significant finding at a p-value of 0.007, none of the SNP-
based tests was significant at a p-value of 0.05. The parameters used to analyze these
findings are $H = 3$ haplotypes, $G = 10$ of the 13 SNPs which vary in these haplotypes,
15 and $C = 10$ possible pairwise comparisons between the 5 haplotype pairs.

Using Eq. 3, the characteristic haplotype contribution to the phenotypic variance,
 σ_H^2 , may be estimated from the haplotype-based ANOVA to be 0.063. Had haplotype-
based regression been performed instead of ANOVA, use of Eq. 1 predicts that a p-value
of 0.008 would have been observed. Although the small number of haplotypes suggests
20 strong linkage disequilibrium between SNPs, sequence data presented by Martin and
coworkers demonstrates that correlation between SNPs extends no further than one or
two SNPs, in accord with their observation that no SNP correlated perfectly with any
haplotype. Consequently the weak linkage limit, i.e., no SNP correlation, is used to
estimate the expected p-value from a SNP-based regression test. The resulting p-value
25 from Eq. 1, corrected for multiple hypothesis testing, is 0.49, consistent with the reported
lack of significance. The Liggett study is therefore consistent with a model of simple
additive effects from multiple causative SNPs; there is no indication of unique or non-
additive interactions. Although such effects can not be ruled out, it is not likely that this
series of experiments, with insufficient power to detect the simple main effect of
30 individual SNPs, would have sufficient power to detect the interaction terms in an
ANOVA model. Similarly, although a model including haplotype main effects and

haplotype-haplotype interactions would be expected to yield significance for the main effects, it is unlikely that the interaction terms would be significant.

EXAMPLE 2. COMPARISON OF SNP-BASED AND HAPLOTYPE-BASED ASSOCIATION STUDIES

This example provides an illustration of the methods of the invention using data presented in a series of simulations designed to assess the power of various association studies. Long & Langley, Genome Res. 9: 720-731, 1999]. Although the details of the simulation model, including the use of haploid rather than diploid genomes for estimates of the power of haplotype-based association studies, are different from the model considered here, the essence of the model is the same: multiple polymorphic markers exist in linkage disequilibrium with each other and with a quantitative trait nucleus. Long and Langley report, based on their simulations, that tests which consider each single marker in turn have power similar to or greater than haplotype-based tests. The same conclusion is reached with the present analytical results, provided that the total number of haplotypes is larger than the total number of SNPs.

Long and Langley also investigate the effects of increasing marker density relative to a parameter $4Nc$, a measure of the extent of linkage disequilibrium along a chromosome. Once the marker density is comparable to the inverse of this length, the simulation results suggest that it is more powerful to increase the number of individuals genotyped than to increase the number of markers tested. The present findings are similar, with the extent of linkage disequilibrium expressed as the number of consecutive SNPs correlated between different haplotypes. Furthermore, when the SNP density is so high that SNPs form super-SNPs, it is found that additional SNPs may actually decrease the power of a SNP-based test due to the correction for multiple hypothesis testing.

EXAMPLE 3. COMPARISON OF SNP-BASED AND HAPLOTYPE-BASED TESTS USING VARYING NUMBERS OF CAUSATIVE SNPS

A comparison of SNP-based and haplotype-based tests is presented in FIGS. 3A-3F using a fixed total number of SNPs and a varying number of causative SNPs. The

number of total number of SNPs is fixed at 20. The number of causative SNPs is 1 (left panels), 3 (middle panels), or 10 (right panels). The number of haplotypes, H , is varied from 1 to 100 within each panel. The additive variance per SNP is fixed at 0.025. The top series of panels illustrates the expected significance for a fixed population size of 300, and the bottom series illustrates the population size required to attain a p-value of 0.05 (5% false-positive rate including the multiple-testing correction) and a power of 0.8 (20% false-negative rate), for the haplotype-pair ANOVA test (dot-dashed line), the haplotype regression test (dashed line), and the SNP regression test (solid line). Haplotype-based tests and SNP-based tests cross in power when the number of haplotypes is just larger than the number of causative SNPs.

EXAMPLE 4. COMPARISON OF SNP-BASED AND HAPLOTYPE-BASED TESTS USING FIXED TOTAL ADDITIVE VARIANCE

A comparison of SNP-based and haplotype-based tests using fixed total additive variance is presented in FIG. 4. The results of the series is similar to FIG. 3, except the total additive variance is fixed at 0.075, implying an additive variance per SNP that varies from 0.075 (1 causative SNP) to 0.0075 (10 causative SNPs). Haplotype-based tests and SNP-based tests cross in power when the number of haplotypes is just larger than the number of causative SNPs.